



Murdoch
UNIVERSITY

Topic 6 Arrays

ICT167 Principles of
Computer Science



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Objectives

- Know how to declare, create and use **arrays in Java**
- Use the **length** instance variable to ensure that array indexes remain in bounds
- Be able to **pass array element values as parameters**
- Be able to **pass arrays as parameters**
- Be able to write **methods which return arrays**

Objectives

- Be able to include **arrays as instance variables**
- Be able to declare, create and initialise **arrays of objects**
- Understand `==` on arrays
- Be able to implement simple **selection algorithms (searching an array)**
 - Sequential search
 - Binary search

Objectives

- Be able to implement simple **sorting algorithms (sorting an array)**
 - Bubble sort
 - Selection sort
 - Insertion sort
- Be able to define and use **multi-dimensional arrays**

Reading

Savitch: Chapter 7

Arrays in Programming Languages

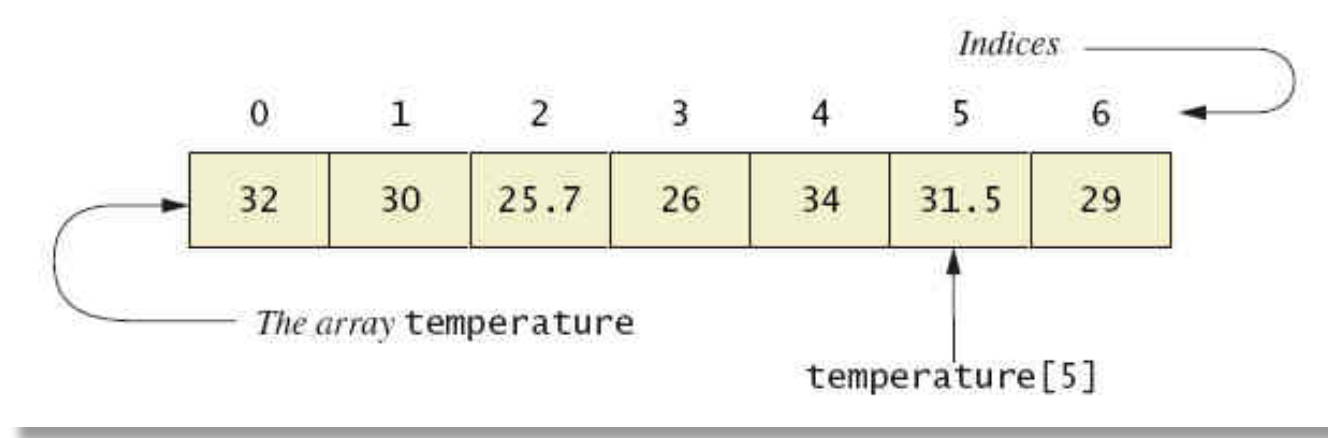
- An array consists of a systematically organised and named sequence of similar variables - called the **elements** of the array
 - That is, it is a single name for a collection of data values, all of the same type
- The elements are numbered: 0, 1, 2, ... and so on, called the **index** (or subscript)
- An array is used in place of a lot of separate variables (which are of the same type)

Arrays in Programming Languages

- An array can be small with only 2 or 3 elements (or even zero), or it can be very large with thousands of elements
- An array is an *ordered collection* of data items
- Each item has a position (or index)
- Each item (except first item) has a unique predecessor
- Each item (except last item) has a unique successor

Visualize Array

- Figure 7.1 A common way to visualize an array



- Note sample program, listing 7.1
class ArrayOfTemperatures

Arrays in Programming Languages

- An array is a *direct access* data structure
- Each item is accessible without going through any other item
- Arrays are the most frequently used data structure

Advantages / Uses of Arrays

- Advantages:
 - Saves thinking up the names for a lot of variables
 - Easy to change/control how many there are
 - Can process them systematically
 - Can be efficiently stored
 - Idea is common to nearly all programming languages
 - In some programming languages, can pass the whole array full of values around to procedures and back

Advantages / Uses of Arrays

- **Restrictions:**
 - Each item in an array must be of the same type
- **Variations between programming languages:**
 - Run-time changing of array size allowed?
 - Checking of bounds?
 - Passing to procedures/methods allowed?
 - Returning from procedures allowed?
 - Pass by reference or value?
 - Arrays of objects or just primitive values?
 - Multi-dimensional?

Creating Arrays in Java

- General syntax for declaring an array:

```
BaseType[] ArrayName= new BaseType[Length];
```

- Examples:

```
// 80-element array with base type char
```

```
char[] symbols = new char[80];
```

```
// 100-element array of doubles:
```

```
double[] readings = new double[100];
```

```
//100-element array of Species:
```

```
Species[] specimen = new Species[100];
```

Creating Arrays in Java

- Length of an array is specified by the number in brackets when it is created with ***new***
 - it determines the amount of memory allocated for the array elements (values)
 - it determines the *maximum* number of elements the array can hold
 - storage is allocated whether or not the elements are assigned values

Creating Arrays in Java

- The array length is established when the array is created
 - It is automatically stored in the (read-only) instance variable length, and cannot be changed
- An array is a special kind of object in Java
- Eg: declare an array of ints:

```
int[] mark;
```

```
// mark is now an “array of int” type variables, with  
// null reference
```

Creating Arrays in Java

- Create an array of int “objects” of a certain length:

```
mark = new int[7];
```

```
// the variable mark now refers to an array of seven ints  
// each one initialised to the default int value of zero
```

- OR, declare and create:

```
int[] mark = new int[7];
```

- Data can now be stored in the array as:

```
mark[0] = 85;
```

Creating Arrays in Java

	[0]	[1]	[2]	[3]	[4]	[5]	[6]
mark:	85	70	50	62	39	92	54

Creating Arrays in Java

- Later on may be make `mark` refer to another array object:

```
mark = new int[9];
```

- Note: This does not change the size of an array
- It just makes the variable refer to a new, bigger array
- The old array is still there, the same size as before, elsewhere in memory

Creating Arrays in Java

- Do somethings with the first element in the array:

```
mark[0] = 30;  
System.out.println(mark[0]);  
mark[0] = keyboard.nextInt();  
System.out.println(mark[4+1-5]);
```

- Do somethings with the last element in the array:

```
mark[8] = 72;  
System.out.println(mark[8]);
```

Creating Arrays in Java

- Output all elements of the array:

```
for (int i=0; i<9; i++)
```

```
    System.out.println(mark[i]);
```

- Note that array subscripts use zero-numbering. That is:
 - the first element has subscript 0
 - the second element has subscript 1
 - the nth element has subscript n-1
 - the last element has subscript length-1

Array Lengths

- Arrays are sort of objects and have a publically accessible (but read-only) instance variable **length**, which gives the number of elements in the array. Eg:

```
mark.length
```

- So a very common form of loop is:

```
for (index=0; index<mark.length; index++) {  
    System.out.println("Enter the "  
        + index + "th mark:");  
    mark[index] = keyboard.nextInt();  
}
```

Array Lengths

- Note: this form of loop is often used to give initial values to the elements of an array but there is a special way of initialising a small array with a list of values
- This is done at the time the array is declared:

```
int[] coins = {5,10,20,50,100,200};  
// implied length = 6  
double[] data = {4.5,4.7,5.1,5.5};  
// implied length = 4
```

Array Lengths

- Subscript out of Range Error:
 - *Note that if the index (inside the [brackets]) evaluates to less than zero, or greater than or equal to the length of the array, then the program will suffer a runtime error:*
`ArrayIndexOutOfBoundsException`

Example

```
/** Read temperatures from the user and shows which are
    above and which are below the average of all the
    temperatures. From Savitch Listing 7.1 */
import java.util.Scanner;
public class ArrayOfTemperatures2 {
    public static void main(String[] args) {
        Scanner keyboard = new Scanner(System.in);
        System.out.println("How many temperatures
                           do " + "you have?");
        int size = keyboard.nextInt();
        double[] temperature = new double[size];
```

Example

```
// Read temp's and compute their average
double sum, average;
System.out.println("Enter " + temperature.length + "
                    temperatures:");

sum = 0;
for(int i = 0;i<temperature.length;i++) {
    temperature[i] = keyboard.nextDouble();
    sum = sum + temperature[i];
} // end for
average = sum/temperature.length;
System.out.println("Avg temp is " + average);
```


Example

```
// Display each temp + its relation to avg
System.out.println("The temperatures are");
for (int i = 0;i<temperature.length;i++) {
    if (temperature[i] < average)
        System.out.println(temperature[i] + "
                                below average.");
    else if (temperature[i] > average)
        System.out.println(temperature[i] + "
                                above average.");
    else //temperature[i] == average
        System.out.println(temperature[i] + " the
                                average.");
} // end for
```

Example

```
        System.out.println("Have a nice week.");  
    } // end main  
} // end class
```

Arrays as Parameters

Passing/Returning Arrays of Primitive types to/from methods

- Passing an array element is like passing any other variable. Eg:

```
double d = Math.sqrt(mark[2]);
```

```
// Primitive passed by value: the value cannot be  
// changed by the method
```

Arrays as Parameters

- Passing a whole array is also possible:

```
public static double avg(int[] arr) {  
    int total = 0;  
    for (int i=0; i < arr.length; i++)  
        total = total + arr[i];  
    return (double)total/arr.length;  
}
```

Arrays as Parameters

- The caller then uses:

```
System.out.print("The average mark is ");  
System.out.println(avg(mark));
```

- In this example, the array `mark` is passed as parameter to the method `avg` which returns the average value of numbers stored in the array
- Within the method `avg`, the array is referred to with the name `arr`

Arrays as Parameters

- *Note that the [brackets] appear in the definition of the method and not in the method call*
- Also note that passing a whole array to a method is done via **pass by reference** (as with other objects) and so that the method is allowed to change the values in the array
- This is useful (for example, if you want to rearrange or sort the values in the array) but be careful

Example: ReturnArrayDemo

```
/** Program to demonstrate a method returning an
    array */
import java.util.Scanner;
public class ReturnArrayDemo {
    public static void main(String arg[]) {
        Scanner keyboard = new Scanner(System.in);
        System.out.println("Enter score on exam 1:");
        int firstScore = keyboard.nextInt();
        int[] nextScore = new int[3];
        int i;
        for (i = 0; i < nextScore.length; i++)
            nextScore[i] = firstScore + 5 * i;
    }
}
```

Example: ReturnArrayDemo

```
double[] averageScore;
double averageScore =
    averageArray(firstScore, nextScore);
for (i = 0; i < nextScore.length; i++) {
    System.out.println("If your score on
        exam 2 is " + nextScore[i]);
    System.out.println("Your average will be
        " + averageScore[i]);
}
} // end main
```


Example: ReturnArrayDemo

```
public static double[] averageArray(int
    firstScore, int[] nextScore) {
    double[] temp=new double[nextScore.length];
    for (int i = 0; i < temp.length; i++)
        temp[i]=average(firstScore,nextScore[i]);
    return temp;
} // end averageArray
public static double average(int n1, int n2){
    return (n1 + n2)/2.0;
} // end average
} // end class ReturnArrayDemo
```

Arrays in Objects

- It is permitted and is very common to have arrays as instance variables in objects
- Eg:
 - a student might have an array of marks
 - a tour operator has an array of guides
 - an alphabet has an array of letters
 - a letter has an array of dots (for printing)
 - a questionnaire has an array of questions
 - a polygonal shape has an array of vertices
 - etc.

Arrays in Objects

- **Eg: in the class Student:**

```
private String familyName;  
private String[] otherNames;  
private long studentNumber;  
private int[] componentMarks;  
private char grade;
```

Objects in Arrays

- It is permitted and is very common to have arrays of objects (as opposed to primitive values)
- Eg:
 - an array of guides
 - an array of products
 - an array of questions
 - an array of vertices
 - an array of students
 - etc.

Objects in Arrays

- Eg: suppose that we have a class `Student` available. A client can use this as follows:

```
Student[] pupil = new Student[50];
```

```
// declares a Student array type variable pupil,
```

```
// creates a Student array object of size 50 and makes
```

```
// pupil refer to this object
```

- Now

```
pupil[0], pupil[1], ..., pupil[49]
```

are all variables that can refer to `Student` objects

Remember: Initialize Elements

- But beware!!

```
pupil[0], pupil[1], ..., pupil[49]
```

```
// are all null reference variables: none of them  
// actually refer to any Student objects yet
```

- If we called:

```
pupil[0].writeDetails();
```

- or even:

```
pupil[0].enterDetails();
```

- then we would get a **NullPointerException**

Remember: Initialize Elements

- Before calling any methods on Student objects you have to create some Student objects. Eg:

```
for (int i=0; i<pupil.length; i++)  
pupil[i] = new Student() ;  
// that is using the default constructor from the  
// Student class for each of the 50 objects
```

- Then you can call:

```
for (int i=0; i<pupil.length; i++){  
System.out.println("Next student's details.");  
pupil[i].enterDetails();  
}
```

Example: Student Class

```
// Student.java
// example Student class with an array of marks
import java.util.Scanner;
public class Student {
    private String name;
    private int[] mark;
    public Student() {
        name = "No name yet.";
        mark = null;
    }
}
```


Example: Student Class

```
public void enterDetails() {
    Scanner keyboard = new Scanner(System.in);
    System.out.print("Name:");
    name = keyboard.nextLine();
    System.out.print("Number of components:");
    int noc = keyboard.nextInt();
    mark = new int[noc];
    for(int i = 0;i < noc;i++) {
        System.out.println("Enter mark for " +(i+1)
                           + "th component:");
        mark[i]= keyboard.nextInt();
    }
}
```

Example: Student Class

```
public void writeDetails() {
    System.out.println("Name:" + name);
    System.out.println("Number of components:"
                       + mark.length);
    for(int i = 0;i < mark.length;i++)
        System.out.println("Mark for " + (i+1)
                           + "th component:" + mark[i]);
    System.out.println("That's all.");
}
```

Example: Student Class

```
public int total() {  
    int sum = 0;  
    for(int i = 0;i < mark.length;i++)  
        sum = sum + mark[i];  
    return sum;  
}  
} // end class Student
```

Example: Client Class

```
//StudentClient.java
// example of client program using the Student class
// and making an array of students
import java.util.Scanner;
public class StudentClient {
    public static void main(String[] args) {
        // array of student objects, currently null
        Student[] pupil;
        // array of total marks, currently null
        int[] tot;
        // array of letter grades, currently null
        char[] grade;
```

Example: Client Class

```
// The above arrays are an example of parallel
// arrays
int nops=0;
Scanner keyboard = new Scanner(System.in);
System.out.println("Welcome to class mark
                                                             helper.");
System.out.println("Please enter number of
                                                             pupils:");

// length of array
nops = keyboard.nextInt();
// create array of type Student; refer to Student
// objects
pupil = new Student[nops];
```

Example: Client Class

```
// create array of ints to store total marks
tot = new int[nops];
// create an array of chars to store grades
grade = new char[nops];
System.out.println("Enter students' details.");
for (int i = 0; i < pupil.length; i++) {
    // very important !!!
    pupil[i] = new Student();
    pupil[i].enterDetails();
    tot[i] = pupil[i].total();
    System.out.println("Total mark for that"
        + " student is "+ tot[i]);
} // end for
```

Example: Client Class

```
double avg = findClassAv(tot);
System.out.println("Pass mark is " + avg);
System.out.println();
System.out.println("Here's the results.");
for (int i = 0; i < pupil.length; i++) {
    if (tot[i] >= avg) grade[i] = 'P';
    else grade[i] = 'F';
    pupil[i].writeDetails();
    System.out.println("Final grade for that" +
        " student is "+ grade[i]);
}
```

Example: Client Class

```
        System.out.println("Thank you, BYE.");
    }//end of main
public static double findClassAv(int[] arr) {
    int sum = 0;
    for (int i =0;i < arr.length;i++)
        sum = sum + arr[i];
    return (double)sum/arr.length;
} //end of findClassAv
} // end class StudentClient
```


Example: Output

```
/* Sample test run:  
Welcome to class mark helper.  
Please enter number of pupils: 2  
Please enter students' details.  
Name: J Blogg  
Number of components: 3  
Enter mark for 1th component: 60  
Enter mark for 2th component: 70  
Enter mark for 3th component: 80  
Thank you.  
The total mark for that student is 210
```

Example: Output

Name: A N Other

Number of components: 3

Enter mark for 1th component: 75

Enter mark for 2th component: 85

Enter mark for 3th component: 90

Thank you.

The total mark for that student is 250

Pass mark is 230.0

Example: Output

Here are the results.

Name: J Blogg

Number of components: 3

Mark for 1th component: 60

Mark for 2th component: 70

Mark for 3th component: 80

That's all.

The final grade for that student is F

Example: Output

Name: A N Other

Number of components: 3

Mark for 1th component: 75

Mark for 2th component: 85

Mark for 3th component: 90

That's all.

The final grade for that student is P

Thank you for using class mark helper.

*/

Checking Arrays for Equality

- Arrays are like objects as far as `==` and `!=` are concerned
- These equality tests will compare the memory addresses of two objects, not the data values that they hold
- If `marks` and `sums` are arrays of the same type, then you can ask:
 - `if (marks == sums) ...`
 - but they are only equal if both variables refer to the same object in memory

Checking Arrays for Equality

- Eg: if you created one object and made marks refer to it:

```
int[] marks = new int[10];  
for (int i=0; i<10; i++)  
    marks[i] = 10-i;
```

- and then you wrote:

```
int[] sums;  
sums = marks;
```

- The == test will hold in the above case

Checking Arrays for Equality

- So, for example, you can have two arrays of ints of the same length with the same numbers in them but they are not equal (according to `==`).
- To test two arrays for equality you need to define an `equals` method that returns true if and only if the arrays have the same length and all their corresponding values are equal
- The code below shows an example of an `equals` method

Checking Arrays for Equality

```
public static boolean equals(int[] a, int[] b) {
    boolean match = true;    // tentatively
    if (a.length != b.length) match = false;
    else {
        int i = 0;
        while (match && (i < a.length)) {
            if (a[i] != b[i])
                match = false;
            i++;
        }
    }
    return match;
}
```


Checking Arrays for Equality

- A method call:

```
boolean same = equals(marks, sums);  
// where marks and sums are int arrays
```

Searching in Arrays

- There are many techniques for searching an array for a particular value
- Sequential search:
 - Start at the beginning of the array and proceed in sequence until either the value is found or the end of the array is reached
 - Or, just as easy, start at the end and work backwards toward the beginning
 - If the array is only partially filled, the search stops when the last meaningful value has been checked

Searching in Arrays

- It is not the most efficient method to search an array but it works and is easy to program
- Can be performed on both unsorted and sorted arrays

Searching in Arrays

```
public static boolean search(int[] a, int item) {
    boolean found = false;
    if (a.length > 0) {
        int i = 0;
        while (!found) && (i < a.length) {
            if (a[i] == item) found = true;
            i++;
        }
    }
    return found;
}
```

Searching in Arrays

■ A method call:

```
boolean itemFound = search(array, num);  
if (itemFound)  
    System.out.println ("The value " + num + "  
                        exists in the array");  
else  
    System.out.println ("The value " + num + "  
                        is not found in the array");
```

Searching in Arrays

- It is common to have to find (or select) the maximum element in an array. Eg:

```
int indexOfMaxSoFar = 0;
for (int i = 1; i < arr.length; i++)
    if (arr[i] > arr[indexOfMaxSoFar])
        indexOfMaxSoFar = i;
indexOfMax = indexOfMaxSoFar;
```

Searching in Arrays

- Note this assumes that there is at least one element in the array
- Variations on this idea will find the minimum element, or the second biggest, etc.
- Notice that we make about 100 comparisons to find the maximum element in a list of 100 numbers, etc.

Sorting Algorithms

- It is also very common to have to sort a whole array of values into some order (numeric, alphabetical), including having to sort an array of complex objects into order according to a complex ordering relationship
 - Eg: sort by surname and then by given name (for people with the same surname, etc)
- This is a very important problem in computing and it has been well studied

Sorting Algorithms

- It can be complicated and there are several general approaches. Eg:
 - bubble sort
 - insertion sort
 - selection sort
 - quick sort
- It is good practice for a beginner programmer to make a working sorting program; it is not too hard

Sorting Algorithms

- However, the easiest approaches give inefficient programs
 - Eg: bubble sort might take 1 million moves to sort 1,000 entries
- If program speed is more important than programmer effort (and debugging time, etc.) then use quicksort which will take about 10,000 moves to sort 1,000 entries

Selection Sort

- One of many algorithms for sorting data items in ascending or descending order
- Selection sort method:
- Repeat
 - Find the *largest* item in the *unsorted* array
 - Swap it with the *last* item in the *unsorted* array
 - Reduce the unsorted array size by 1
- Until the array is sorted

Selection Sort

- Array to sort

Pass 1:	43	22	17	36	16
Pass 2:	16	22	17	36	43
Pass 3:	16	22	17	36	43
Pass 4:	16	17	22	36	43

Selection Sort

- In the above example, there are four passes needed to sort a list of five data items
- A variation on the above method is to find the *smallest* item in the unsorted array, swap it with the *first* item in the unsorted array, reduce the unsorted array size by 1
 - Repeat until the array is sorted

Selection Sort

```
// SelectSortV1.java
// To sort an array using Selection Sort
public class SelectSortV1 {
    public static void main( String[] args) {
        int[] anArray =
            {98,76,65,105,45,1,199,15,88,100};
        // sort the array in ascending order:
        SortArrayBySelection (anArray);
        // output the sorted numbers:
        System.out.println("Sorted numbers are:");
        for (int i = 0;i < anArray.length;i++)
            System.out.println( anArray[i]);
        System.out.println("End program - Bye.");
    } // end main
```

Selection Sort

```
public static void SortArrayBySelection(int[]
                                     arrayToSort) {
    int indexOfLargest, last, temp;
    for (last = arrayToSort.length-1; last >= 1;
         last--) {
        indexOfLargest = 0;
        // find index of largest in unsorted array
        for (int i = 1; i <= last; i++)
            if (arrayToSort[i] >
                arrayToSort[indexOfLargest])
                indexOfLargest = i;
        // end if
    } // end i for
}
```

Selection Sort

```
// swap largest with last
temp = arrayToSort[last];
arrayToSort[last] =
    arrayToSort[indexOfLargest];
arrayToSort[indexOfLargest] = temp;
} // end outer for
} // end method SortArrayBySelection
} // end of class SelectSortV1
```


Selection Sort

```
/* Output  
The sorted numbers are:  
1  
15  
45  
65  
76  
88  
98  
100  
105  
199  
End of program - Bye.  
*/
```

Insertion Sort

- Another example of an easy algorithm to sort an array of integers of into ascending order:

```
for i = 1 to arrayLength-1
  temp = arr[i]
  j = 0
  while (temp > arr[j])
    j = j+1
  end while
  for k=i downto j
    arr[k] = arr[k-1]
  end k for
  arr[j] = temp
end i for
```

Insertion Sort

- Each element is copied and inserted into the correct position in the array
- After the i th pass through the loop-body the first $i+1$ elements are in order
- During the i th pass, the value $arr[i]$ is put in its right place amongst the first $i+1$ elements by finding the place and then moving all the rest of the sorted values along one place: that is, $arr[i]$ is inserted in its right place

Step 1		Checking second element of array with element before it and inserting it in proper position. In this case, 3 is inserted in position of 12.
Step 2		Checking third element of array with elements before it and inserting it in proper position. In this case, 1 is inserted in position of 3.
Step 3		Checking fourth element of array with elements before it and inserting it in proper position. In this case, 5 is inserted in position of 12.
Step 4		Checking fifth element of array with elements before it and inserting it in proper position. In this case, 8 is inserted in position of 12.
		Sorted Array in Ascending Order

Figure: Sorting Array in Ascending Order Using Insertion Sort Algorithm

Insertion Sort

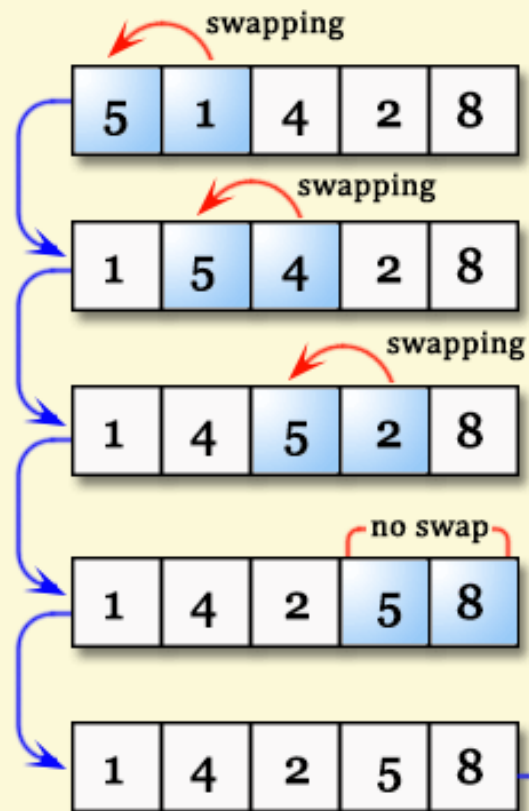
- **EXERCISE IN TOPIC 7**
 - Write down the array contents at every step during the sorting of the values, 12, 18, 2, -4, 17, 12 using insertion sort
 - Note down how many comparisons were made between values

Bubble Sort

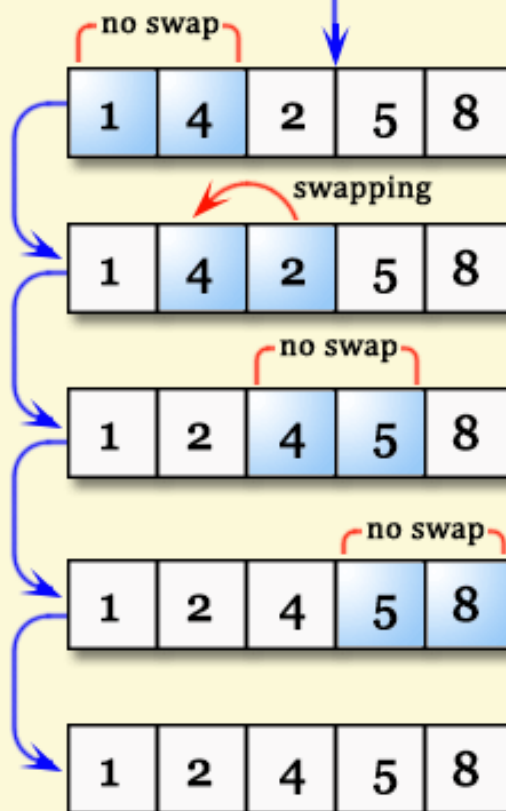
- Also known as *sinking sort* because the smaller values in the array gradually bubble their way towards the top of the array (towards index 0), if sorting in ascending order
- This sorting involves several passes through the array
- On each pass, successive pairs are compared
- If the pairs are in decreasing order they are swapped

Bubble Sorting

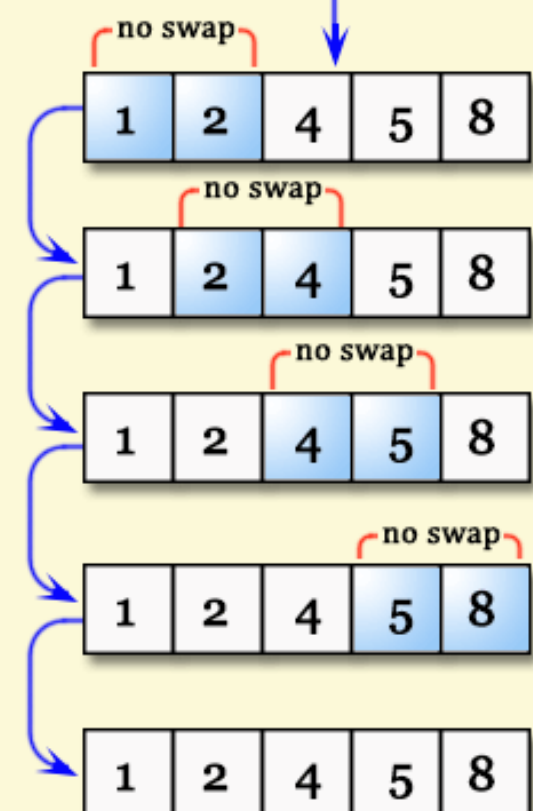
First Pass



Second Pass



Third Pass



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Bubble Sort

```
// bubblesort.java
// To sort an array using Bubble Sort
public class bubblesort {
    public static void main(String[] args) {
        int[] anArray = {10, 9, 8, 7, 6, 5, 4, 3, 2, 1, 0, -1};
        // sort the array in ascending order:
        SortArrayByBubbleSort(anArray);
        // output the sorted numbers:
        System.out.println("The sorted numbers are:");
        for (int i = 0; i < anArray.length; i++)
            System.out.println(anArray[i]);
        System.out.println("End program: Bye.");
    } // end main
}
```


Bubble Sort

```
public static void SortArrayByBubbleSort(  
                                        int[] arrayToSort) {  
    // number of passes  
    for(int i = 1; i < arrayToSort.length; i++) {  
        // perform one pass  
        for(int j=0; j<arrayToSort.length-1; j++)  
            // perform one comparison  
            if (arrayToSort[j]>arrayToSort[j+1])  
                swap (arrayToSort, j, j+1);  
    } // end i for  
} // end method SortArrayByBubbleSort
```

Bubble Sort

```
public static void swap (int[]a, int first,
                        int second)
{
    int temp;
    temp = a[first];
    a[first] = a[second];
    a[second] = temp;
} // end method swap
} //end of class bubblesort
```

Bubble Sort

```
/* Output
The sorted numbers are:
-1
0
1
2
3
4
5
6
7
8
9
10
End of program - Bye.
*/
```

Another Searching Algorithm: Binary Search

- Binary Search:
 - Can only be performed on sorted arrays
 - Much faster than linear searching but more complex
 - The search item is compared against the value of middle element of the array
 - If search item $<$ middle element of array, search is restricted to first half of the array, and so on ...
 - If search item $>$ middle element of array, search second half of the array, and so on ...
 - If search item = middle element, search is complete
 - Thus, each subsequent pass divides the array by half

Another Searching Algorithm: Binary Search

```
/** Binary Search searches a sorted array
```

```
Assumes the array is sorted in ascending order. If  
search is successful, an index of the array where  
target key is found will be returned, otherwise the  
value -1 will be returned */
```

```
public int binarySearch(int arr[], int key) {  
    int first = 0;  
    int last = ar.length - 1;  
    int mid;  
    while (first <= last) {  
        mid = (first + last) / 2;
```

Another Searching Algorithm: Binary Search

```
    if (key == arr[mid])    // match found
        return mid;        // exit
    else if (key < arr[mid]) // search low end
        last = mid - 1;
    else                    //search high end of array
        first = mid + 1;
} // end while
return -1; // match not found
} // end binarySearch
```

Multi-Dimensional Arrays

- These are arrays with more than one index
 - The number of dimensions = number of indexes
- Arrays with more than two dimensions are a simple extension of two-dimensional (2-D) arrays
- Java allows multi-dimensional arrays to be used.
 - An array is n-dimensional if it uses n indexes
 - Up to now we have been studying one-dimensional arrays

Multi-Dimensional Arrays

- A 2-D array corresponds to a table or grid
 - One dimension is the row
 - The other dimension is the column
 - Cell = an intersection of a row and column
 - An array element corresponds to a cell in the table
- The syntax for 2-D arrays is similar to 1-D arrays:

```
Base_Type[][] arrayName = new  
    Base_Type[intExp1][intExp2];
```


Multi-Dimensional Arrays

- Eg: declare a 2-D array of `ints` named `table`, the table is to have ten rows and six columns:

```
int[][]table = new int[10][6];
```

- To access a component of a 2-dimensional array:

```
arrayName[indexExp1][indexExp2];
```

// where:

```
intExp1, intExp2 >= 0
```

```
indexExp1 = row position
```

```
indexExp2 = column position
```

Multi-Dimensional Arrays

- Eg:

```
table[1][2] = 0;
```

```
// initialises the cell (element) in the second row and  
// third column of table to zero
```

- **Usage:** Often we want to store values according to a more complex indexing system.

Eg:

- The time of the i th competitor in the j th race
- The rainfall on the d th day of the m th month of the y th year
- The value in the r th row and c th column of the t th table in the b th book of tables

Multi-Dimensional Arrays

- The examples above are 2, 3 and 4 dimensional respectively

- Eg:

```
int[][] matrix = new int[20][10];  
for (int row=0;row<20;row++)  
    for(int column=0;column <10;column++)  
        matrix[row][column] = row*column;
```

Multi-Dimensional Arrays

- Eg:

```
int[][][] rain = new int[31][12][100];
// initialise all elements of array rain to zero
for (int i=0;i < 31;i++)
    for (int j=0;j < 12;j++)
        for (int k=0;k < 100;k++)
            rain[i][j][k] = 0;
// display the value of one element of array rain
System.out.println("Rainfall on the second of
    January 26 is " + rain[1][0][62] + " cm");
```

Multi-Dimensional Arrays

- The indexed variables (array elements) for multi-dimensional arrays are just like indexed variables for 1-d arrays, except that they have multiple indexes

Example

```
/** Displays a 2-D table showing how interest rates
    affect bank balances. From Savitch (7th ed) pp.579-583
    */
public class InterestTable2 {
    public static final int ROWS = 10;
    public static final int COLUMNS = 6;
    public static void main(String[] args) {
        int[][] table = new int[ROWS][COLUMNS];
        int row, col;
        for (row = 0; row < ROWS; row++)
            for (col = 0; col < COLUMNS; col++)
```

Example

```
table[row][col]=
    getBalance(1000.00,row+1,
                (5 + 0.5 * col));
System.out.println("Balances for Various
                    Interest Rates");
System.out.println("Compounded Annually");
System.out.println("(Rounded to Whole Dollar
Amounts)");
System.out.println("Years 5.00% 5.50% 6.00%
                    6.50% 7.00% 7.50%");
System.out.println();
showTable(table);
} // end main
```

Example

```
/** Pre-condition: Array displayArray has ROWS rows and
    COLUMNS columns
    Post-condition: Array contents displayed with $ signs
    */

public static void showTable(int[][] anArray) {
    int row, column;
    for (row = 0; row < ROWS; row++) {
        System.out.print((row + 1) + "          ");
        for (col = 0; col < COLUMNS; col++)
            System.out.print("$" +
                               anArray[row][column] + "  ");
        System.out.println();
    }
} // end showTable
```


Example

```
/** Returns the balance in an account after a given
    number of years and interest rate with an initial
    balance of startBalance. Interest is compounded
    annually. The balance is rounded to a whole
    number.*/
public static int getBalance(double
    startBalance, int years, double rate) {
    double runningBalance = startBalance;
    int count;
    for (count = 1; count <= years; count++)
        runningBalance=runningBalance*(1+rate/100);
    return (int) (Math.round(runningBalance));
} // end getBalance
} // end class InterestTable2
```

Example

OUTPUT (from InterestTable2) :

Balances for Various Interest Rates
Compounded Annually

(Rounded to Whole Dollar Amounts)

Years	5.00%	5.50%	6.00%	6.50%	7.00%	7.50%
1	\$1050	\$1055	\$1060	\$1065	\$1070	\$1075
2	\$1103	\$1113	\$1124	\$1134	\$1145	\$1156
3	\$1158	\$1174	\$1191	\$1208	\$1225	\$1242
4	\$1216	\$1239	\$1262	\$1286	\$1311	\$1335
5	\$1276	\$1307	\$1338	\$1370	\$1403	\$1436
6	\$1340	\$1379	\$1419	\$1459	\$1501	\$1543
7	\$1407	\$1455	\$1504	\$1554	\$1606	\$1659
8	\$1477	\$1535	\$1594	\$1655	\$1718	\$1783
9	\$1551	\$1619	\$1689	\$1763	\$1838	\$1917
10	\$1629	\$1708	\$1791	\$1877	\$1967	\$2061

Implementation of Multi-Dimensional Arrays

- In Java multi-dimensional arrays are implemented using 1-d arrays
 - That is, multidimensional arrays are arrays of arrays
- With this knowledge, we can use the `length` instance variable to process multi-dimensional arrays
- For example, the following code from the `main` method in class `InterestTable2`

Implementation of Multi-Dimensional Arrays

```
for (row = 0; row < ROWS; row++)  
    for (col = 0; col < COLUMNS; col++)  
        table[row][col] =  
            computeBalance(1000.00, row+1,  
                            (5 + 0.5*column));
```

// can be written as

```
for (row = 0; row < table.length; row++)  
    for (col = 0; col < table[row].length; col++)  
        table[row][col] =  
            computeBalance(1000.00, row+1,  
                            (5 + 0.5*column));
```

Implementation of Multi-Dimensional Arrays

- This means that `table` is actually a 1-d array of length 10, and each of the 10 indexed variables `table[0]` to `table[9]` is a 1-d array of length 6
- Thus the array `table` is an array of arrays

Implementation of Multi-Dimensional Arrays

- Its declaration

```
int[][] table = new int[10][6];
```

is equivalent to the following:

```
int[][] table;
```

```
table = new int[10][];
```

```
table[0] = new int[6];
```

```
table[1] = new int[6];
```

```
. . . . .
```

```
table[9] = new int[6];
```

Implementation of Multi-Dimensional Arrays

- Since a 2-d array in Java is an array of arrays, there is no need for each row to have the same number of elements
- That is, rows can have different number of columns
- Such arrays are called **ragged arrays**

Implementation of Multi-Dimensional Arrays

- Eg:

```
int[][] raggedTable;  
raggedTable = new int[3][];  
raggedTable[0] = new int[2];  
raggedTable[1] = new int[5];  
raggedTable[2] = new int[7];
```


Another Example of 2-D Arrays

```
// TwoDimArrayV2.java modified from Deitel and Deitel
// First dimension (rows) represents number of students
// Second dimension (columns) represents number of
    scores
// per student
public class TwoDimArrayV2 {
    public static void main(String[] args) {
        int scores[][] = {{57, 74, 55, 67},
                           {35, 60, 62, 54},
                           {73, 82, 95, 87}};

        // 3 students, 4 scores per student
        int students, minScore, maxScore;
```

Another Example of 2-D Arrays

```
displayArray (scores); // output the array
// find the minimum and the maximum scores
minScore = findMinimum(scores);
maxScore = findMaximum(scores);
System.out.println("Lowest score: " + minScore
    + "\nHighest score: " + maxScore + "\n" );
// find and display the average score
students = scores.length; // no of students
for (int i = 0; i < students; i++)
    System.out.println("Average for student "+i
        + " is " + findAverage(scores[i]) );
System.out.println ("\nEnd of program - bye.");
} // end main
```

Another Example of 2-D Arrays

```
// find the minimum score
public static int findMinimum(int[][]
                                studentArray)
{
    int min = 100;
    int students, exams;
    students = studentArray.length;
    exams = studentArray[0].length;
    for(int i = 0; i < students; i++) // each student
        for (int j = 0; j < exams; j++) // each grade
            if (studentArray[i][j] < min)
                min = studentArray[i][j];
    return min;
} // end findMinimum
```

Another Example of 2-D Arrays

```
// find the maximum grade
public static int findMaximum(int[][]
                                studentArray)
{
    int max = 0;
    for(int i = 0; i < studentArray.length; i++)
        // for each student
        for(int j = 0; j < studentArray[i].length; j++)
            // for each grade
            if (studentArray[i][j] > max)
                max = studentArray[i][j];
    return max;
} // end findMaximum
```

Another Example of 2-D Arrays

```
// avg score for particular student (or set of scores)
public static double findAverage(int
                                setOfScores[])
{
    int total = 0;
    double average;
    for (int i = 0; i < setOfScores.length; i++)
        total = total + setOfScores[ i ];
    average = (double)total/setOfScores.length;
    return average;
} // end findAverage
```

Another Example of 2-D Arrays

```
// builds up array in string variable and displays it
public static void displayArray(int[][]
                                studentArray) {
    // used to align column heads
    String output = "          ";
    for (int i=0;i<studentArray[0].length;i++)
        // no of columns
        output = output + "[" + i + "]"  ";
}
```

Another Example of 2-D Arrays

```
for (int i=0;i<studentArray.length; i++) {
    // for each row
    output = output+"\nscores[" + i + "]"  ";
    for(int j=0;j<studentArray[0].length;j++)
        output=output+studentArray[i][j]+"  ";
} // end for
System.out.println("\nThe array is:\n");
System.out.println(output);
} // end displayArray
} // end class TwoDimArray
```

Another Example of 2-D Arrays

```
/* OUTPUT
```

```
The array is:
```

```
          [0]   [1]   [2]   [3]
scores[0]   57   74   55   67
scores[1]   35   60   62   54
scores[2]   73   82   95   87
Lowest score: 35
Highest score: 95
Average for student 0 is 63.25
Average for student 1 is 52.75
Average for student 2 is 84.25
End of program - bye.
```

```
*/
```


A red decorative shape on the left side of the slide, consisting of a vertical bar with a diagonal cut at the top.

End of Topic 6